Example 6

Analysis of a tank resting on *Winkler's* medium

Contents Page

1 Description of the problem

An example of an axi-symmetrically circular cylindrical tank resting on elastic foundation using *Winkler's* model is selected to illustrate some features of *ELPLA* for analyzing shell elements.

2 Tank geometry and properties

A circular cylindrical tank of an inner diameter of d = 13 [m] and a height of H = 3.5 [m] is considered as shown in Figure 6.1. Thickness of the tank wall is t = 0.175 [m]. The tank is filled with water. The soil under the base of the tank is represented by isolated springs of stiffness k_s, which represent modulus of subgrade reaction. The tank material, unit weight of the water and the modulus of subgrade reaction are listed in Table 6.1.

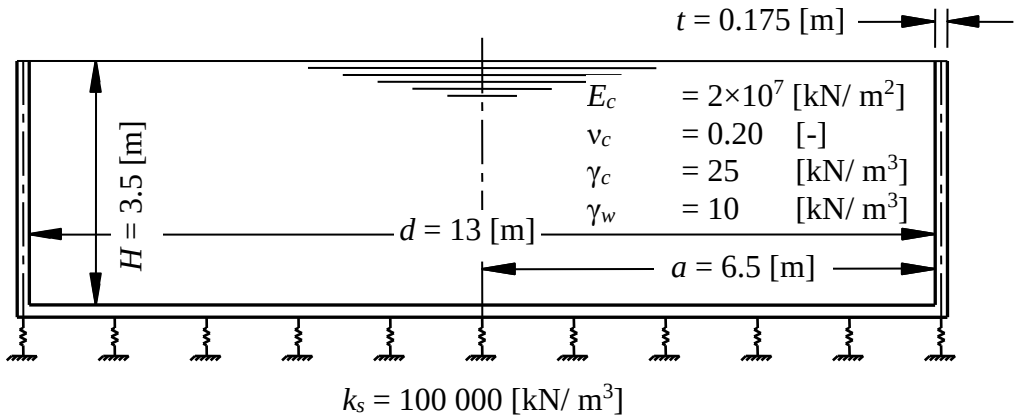

Figure 6.1 Circular cylindrical tank resting on isolated springs with dimensions

Table 6.1 Tank material, water unit weight and modulus of subgrade reaction

Modulus of Elasticity of the tank material	E_c	= 2×10^7	[kN/ m^2]
Poisson's ratio of the tank material	ν_c	= 0.2	[-]
Unit weight of the tank material	γ_c	= 25	[kN/ m^3]
Unit weight of the water	γ_w	= 10	[kN/ m^3]
Modulus of subgrade reaction	k_s	= 100 000	[kN/ m^3]

3 Numerical Analysis

In order to analyze the tank, the height of the tank is divided into 35 equal segments, each of 0.10 [m], as shown in Figure 6.2. The base of the tank is divided into 50 equal segments, each of 0.13 [m].

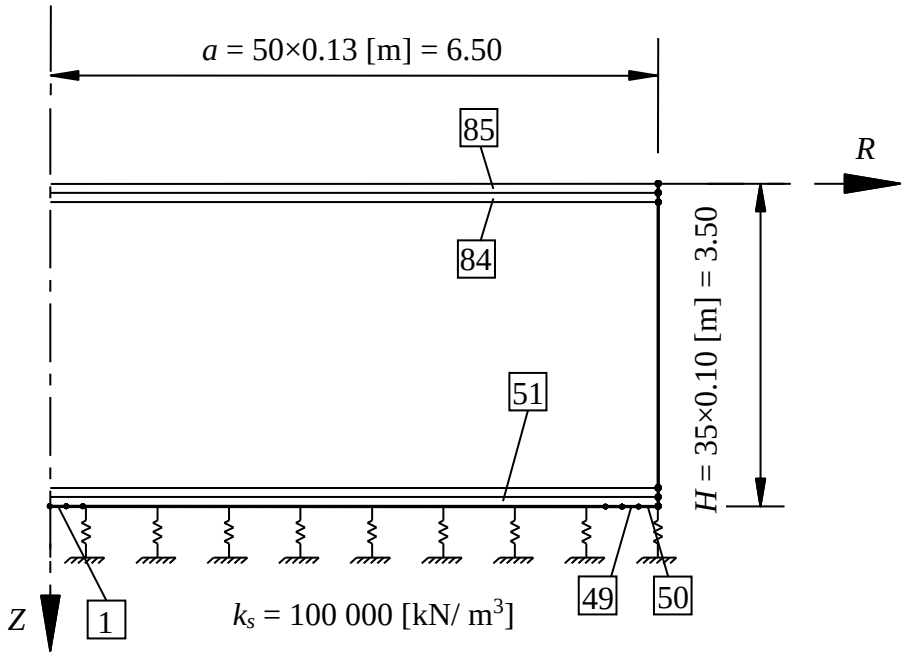

Figure 6.2 Finite element mesh of the tank

4 Creating the project

In this section, the user will learn how to create a project for analyzing an axi-symmetrically circular cylindrical tank resting on elastic foundation using *Winkler's* model. The project will be processed gradually to show the possibilities and abilities of the program. To enter the data of the example, follow the instructions and steps in the next paragraphs.

4.1 Calculation method

Choose "New Project" command from the "File" menu. The following "Calculation Methods" wizard appears, Figure 6.3. This wizard will help the user to define the analysis type and the calculation method of the problem through a series of Forms. The first Form of "Calculation Methods" wizard is the "Analysis Type" Form (Figure 6.3).

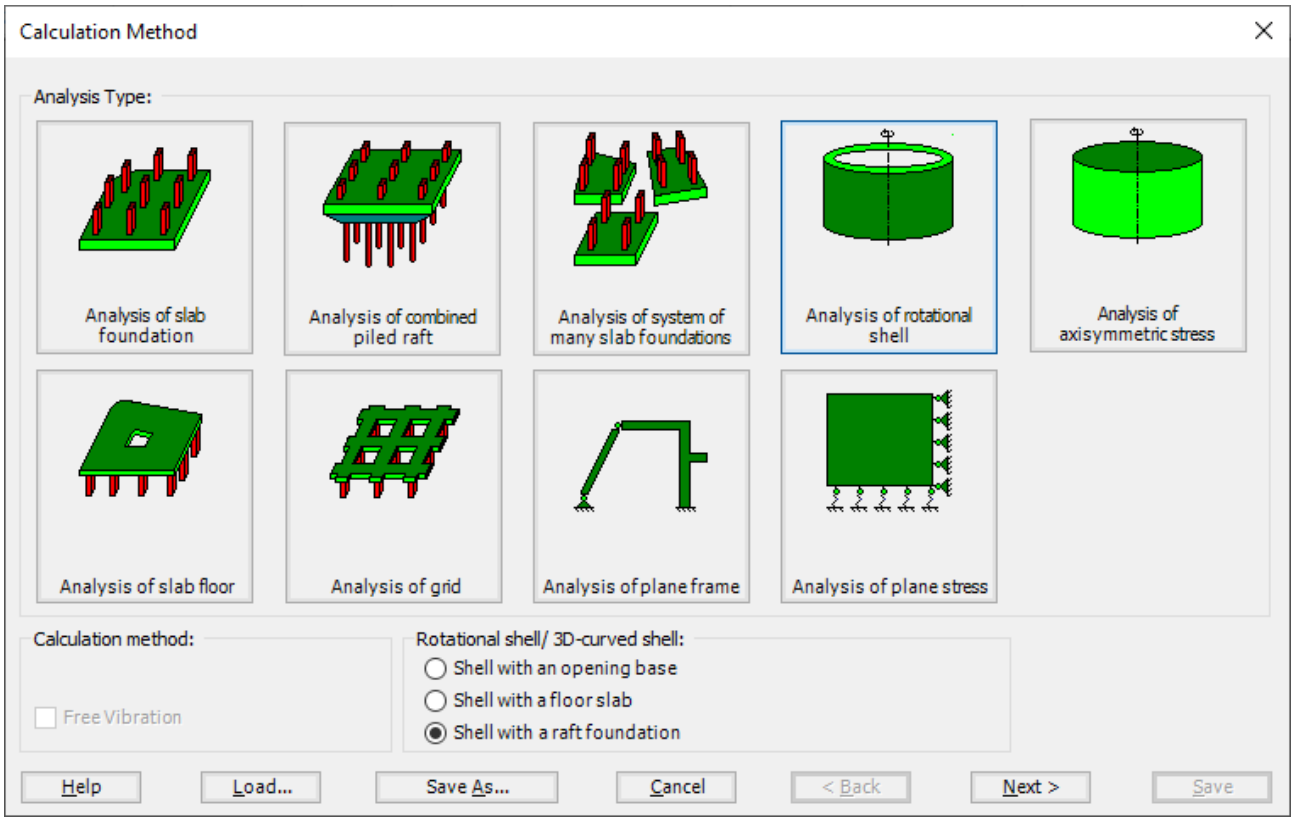

Figure 6.3 "Analysis Type" Form

In the "Analysis Type" Form in Figure 6.3, define the analysis type of the problem. As the analysis type is a circular cylindrical tank problem, select "Analysis of rotational Shell" button, and check "Shell with a raft foundation" option, then click "Next" button to go to the next Form. After clicking "Next" button, the "Calculation Methods" Form appears, Figure 6.4.

To define the calculation method:

- Select the calculation method "2/3 Constant/ Variable Modulus of Subgrade Reaction"
- To determine the modulus of subgrade reaction, select "Modulus is defined by the user"
- Click "Next" button to go to the next Form

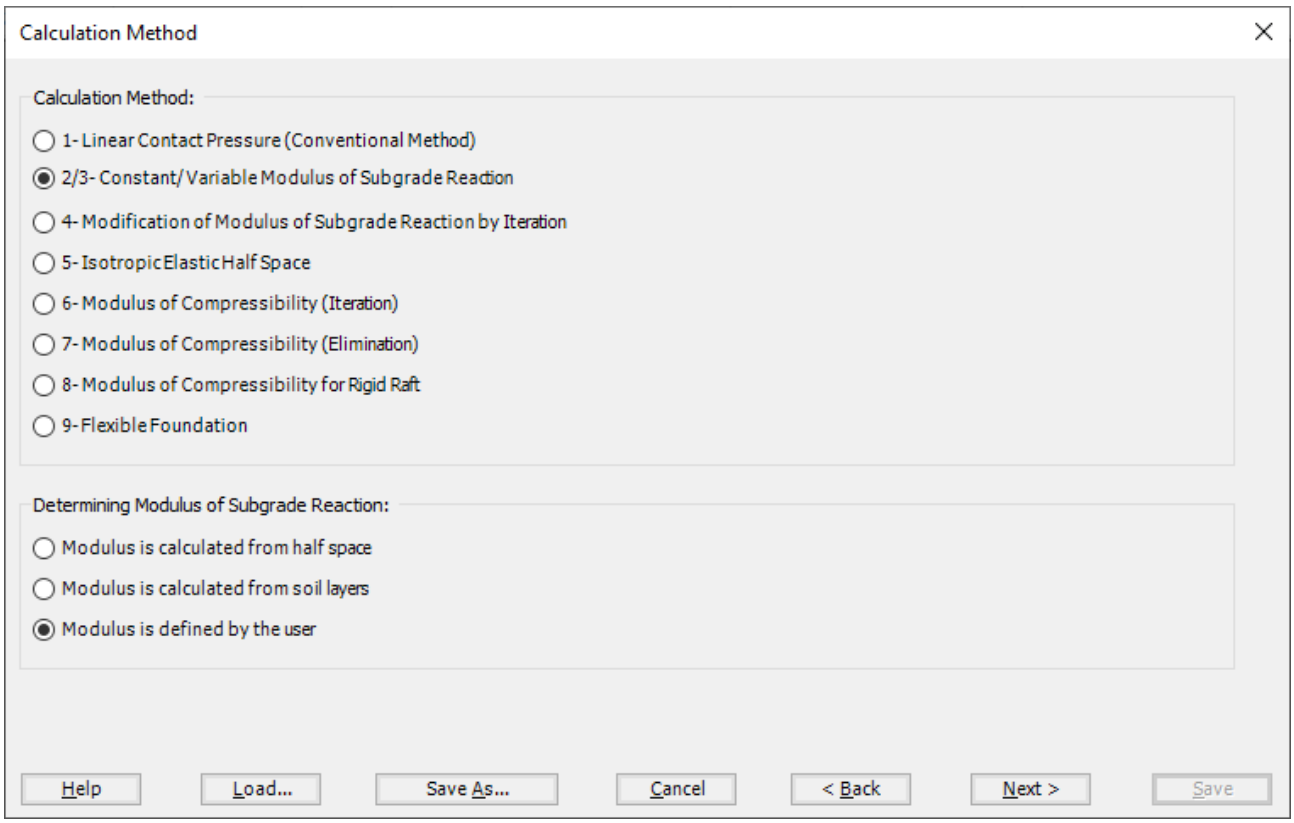

Figure 6.4 "Calculation Method" Form

The last Form in the wizard is the "Options" Form, Figure 6.5. In this Form, *ELPLA* displays some available options corresponding to the chosen numerical model, which differ from model to other. Since no option will be considered in the analysis, click the "Save" button.

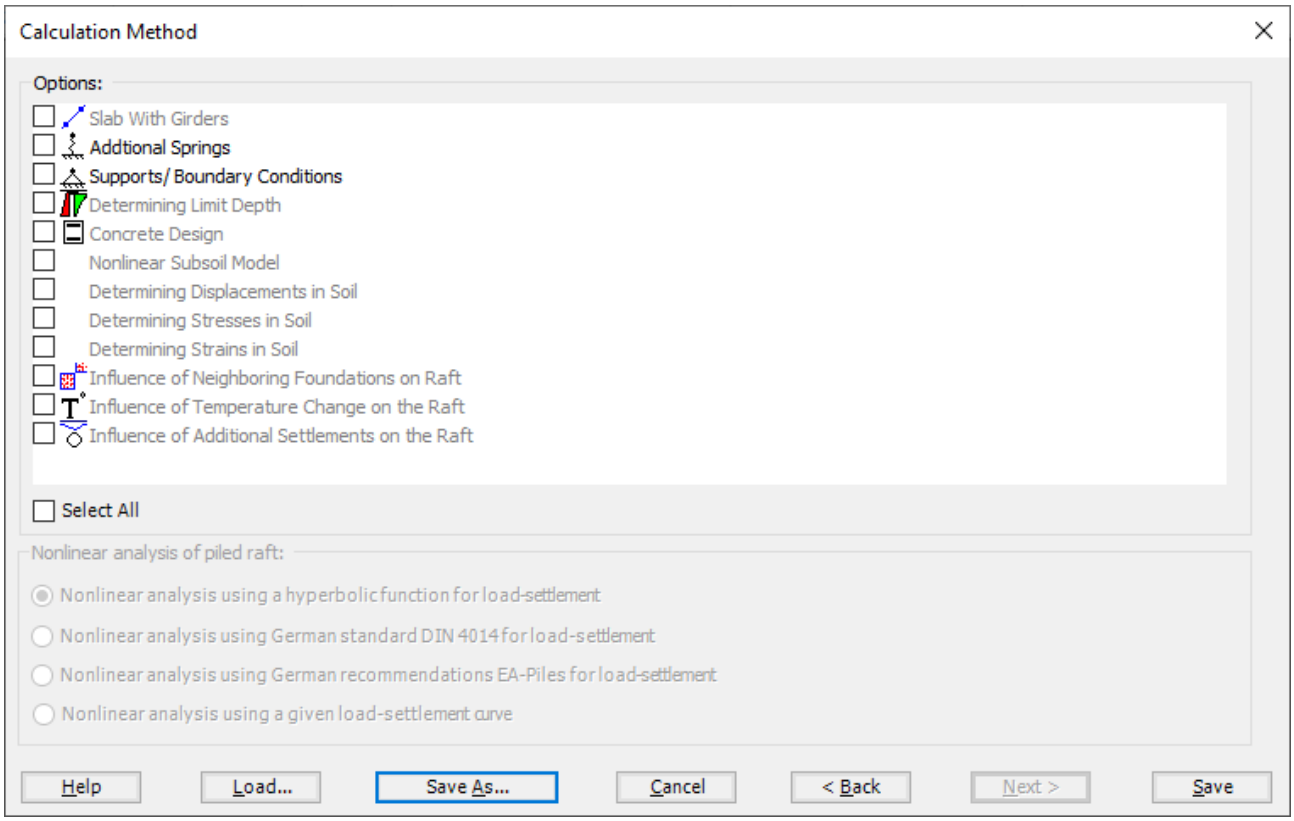

Figure 6.5 "Options" Form

After clicking "Save" button, the "Save as" dialog box appears, Figure 6.6. In this dialog box type a file name for the current project in "File name" edit box. For example, type "Tank on Winkler's medium". *ELPLA* will use automatically this file name in all reading and writing processes.

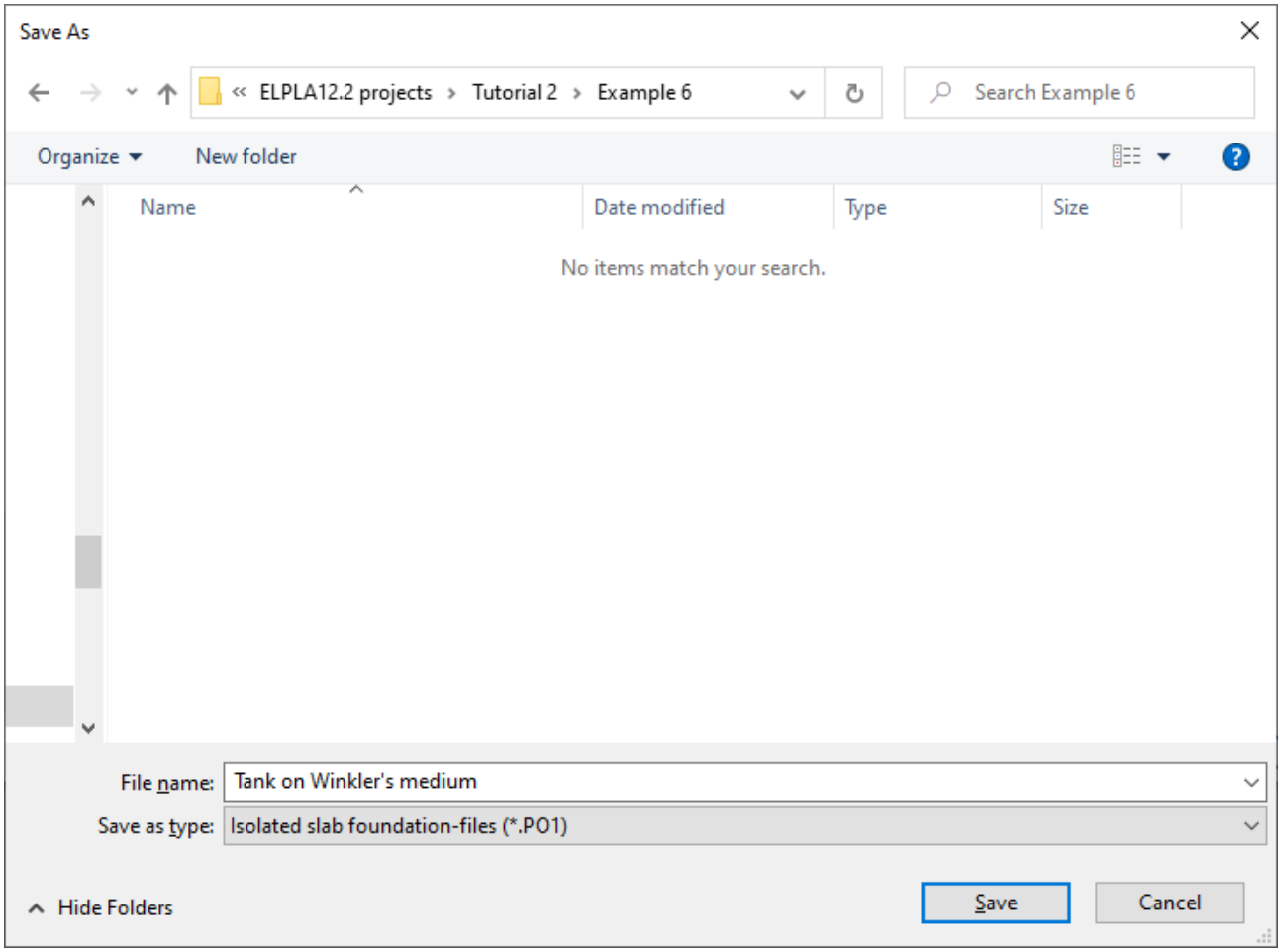

Figure 6.6 "Save as" dialog box

ELPLA will activate the “Data” Tab. In addition, the file name of the current project [Tank on *Winkler's* medium] will be displayed instead of the word [Untitled] in the *ELPLA* title bar.

4.2 Project identification

The user can enter three lines of texts to describe the problem and the basic information about the task. These texts are required only for printing and plotting the data and results. Project identification does not play any role in the analysis. The three lines are optionally and maybe not completely entered. To identify the project, choose "Project Identification" command from the “Data” Tab. The dialog box in Figure 6.7 appears.

In this dialog box

- Type the following line to describe the problem in the "Title" edit box:
  "Analysis of a tank resting on *Winkler's* medium"
- Type the date of the project in the "Date" edit box
- Type the word "Axisymmetric Structures and Tanks" in the "Project" edit box
- Click "Save" button

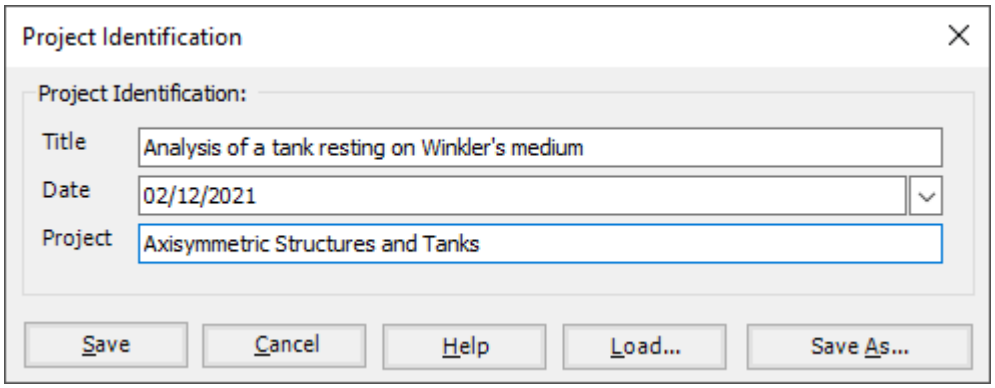

Figure 6.7 "Project Identification" dialog box

4.3 FE-Net data

For the given problem, the tank has an inner diameter of d = 13 [m] and a height of H = 3.5 [m]. the tank height is divided into 35 equal segments, each of 0.10 [m], where the base of the tank is divided into 50 equal segments, each of 0.13 [m]. To define the FE-Net for this tank, choose "FE-Net Data" command from the “Data” Tab. "Analysis of rotational shell" wizard appears as shown in Figure 6.8. This wizard will guide you through the steps required to generate a FE-Net.

The first Form of the wizard is the "Shell type" Form, which contains a group of templates of different shapes of nets. These net templates are used to generate standard nets.

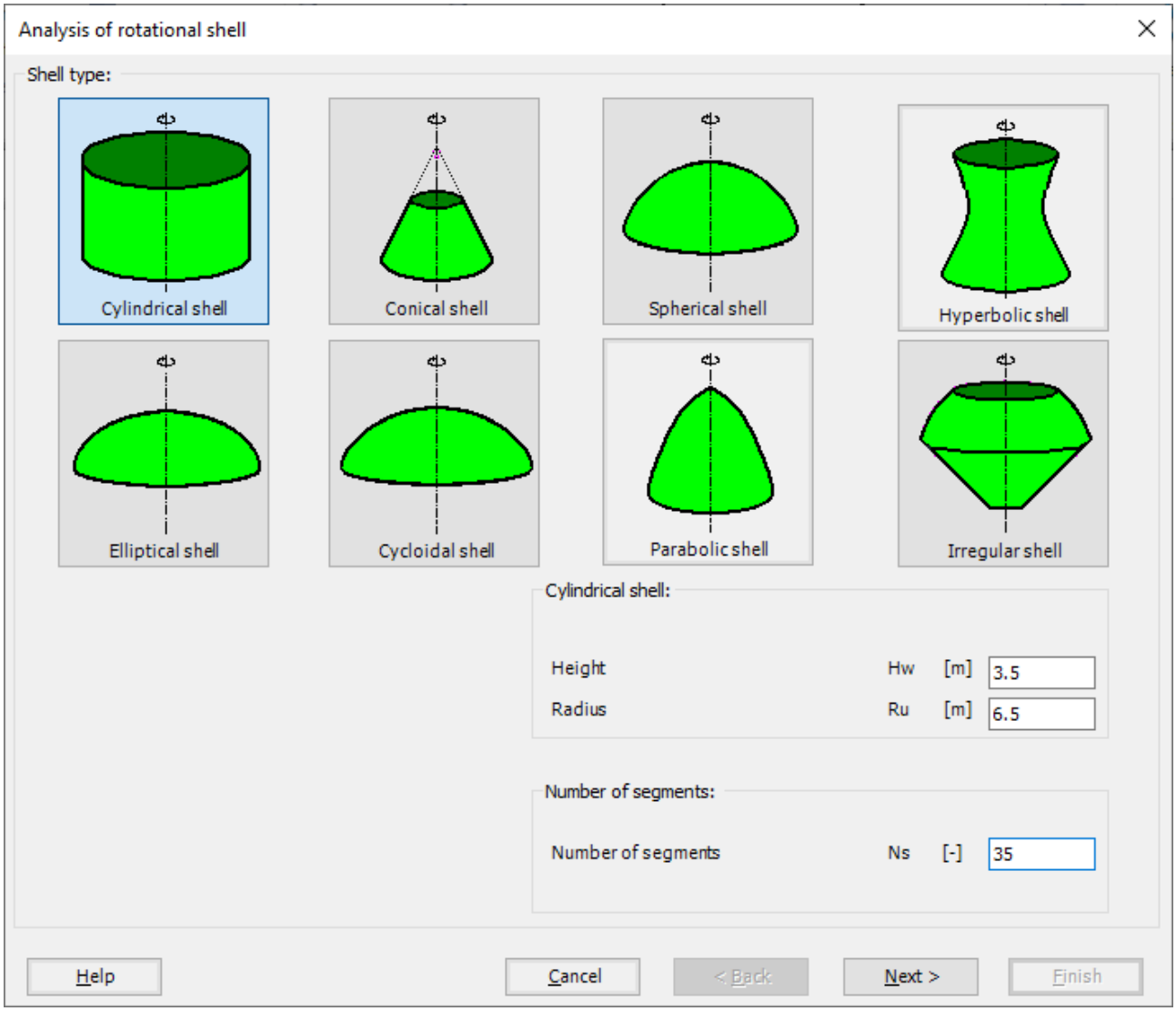

Figure 6.8 "Analysis of rotational shell" wizard with "Shell type" Form

To generate the FE-Net

- In the "Shell type" options choose "Cylindrical shell" button
- Type 3.5 in the "Height" edit box
- Type 6.5 in the "Radius" edit box
- Type 35 in the "Number of segments" edit box
- Click "Next" button to go to the next Form

After clicking "Next" in "Analysis of rotational shell" wizard, the following "Cylindrical shell" Form appears Figure 6.9, *ELPLA* divides the height of the tank into 35 equal segments, the user can edit the data of the segments individually by using "Modify" button, or all of them by using "In Table" button, if it is necessary.

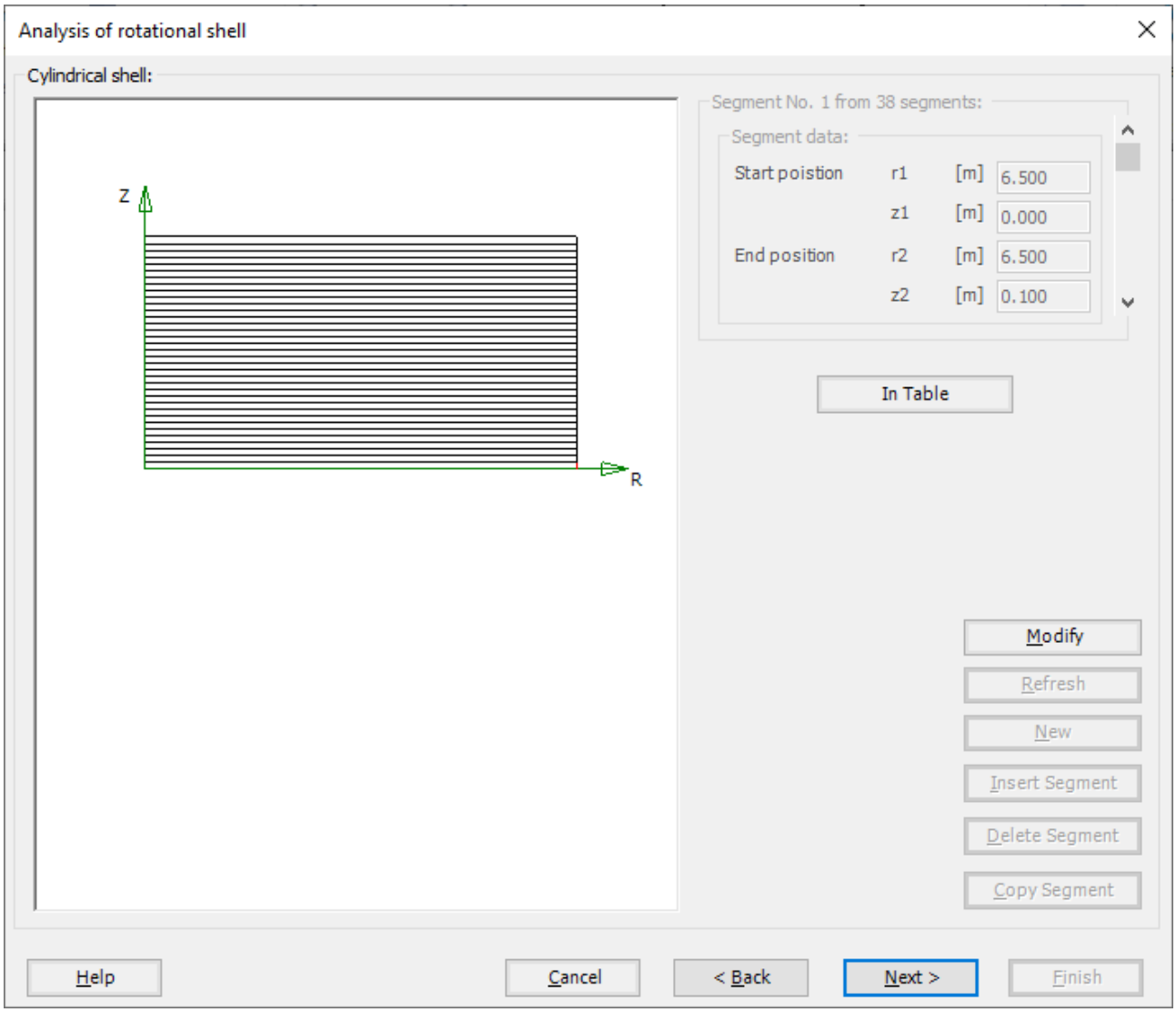

Figure 6.9 "Cylindrical shell" Form

After clicking "Next" in "Analysis of rotational shell" wizard, the following "Net of Base" Form appears Figure 6.10.

To edit the grid spacing in *x*-direction, do the following steps in "Grid in *x*-direction" frame:

- Choose "Constant grid interval" check box
- Type 50 in the "No. of grid intervals" edit box

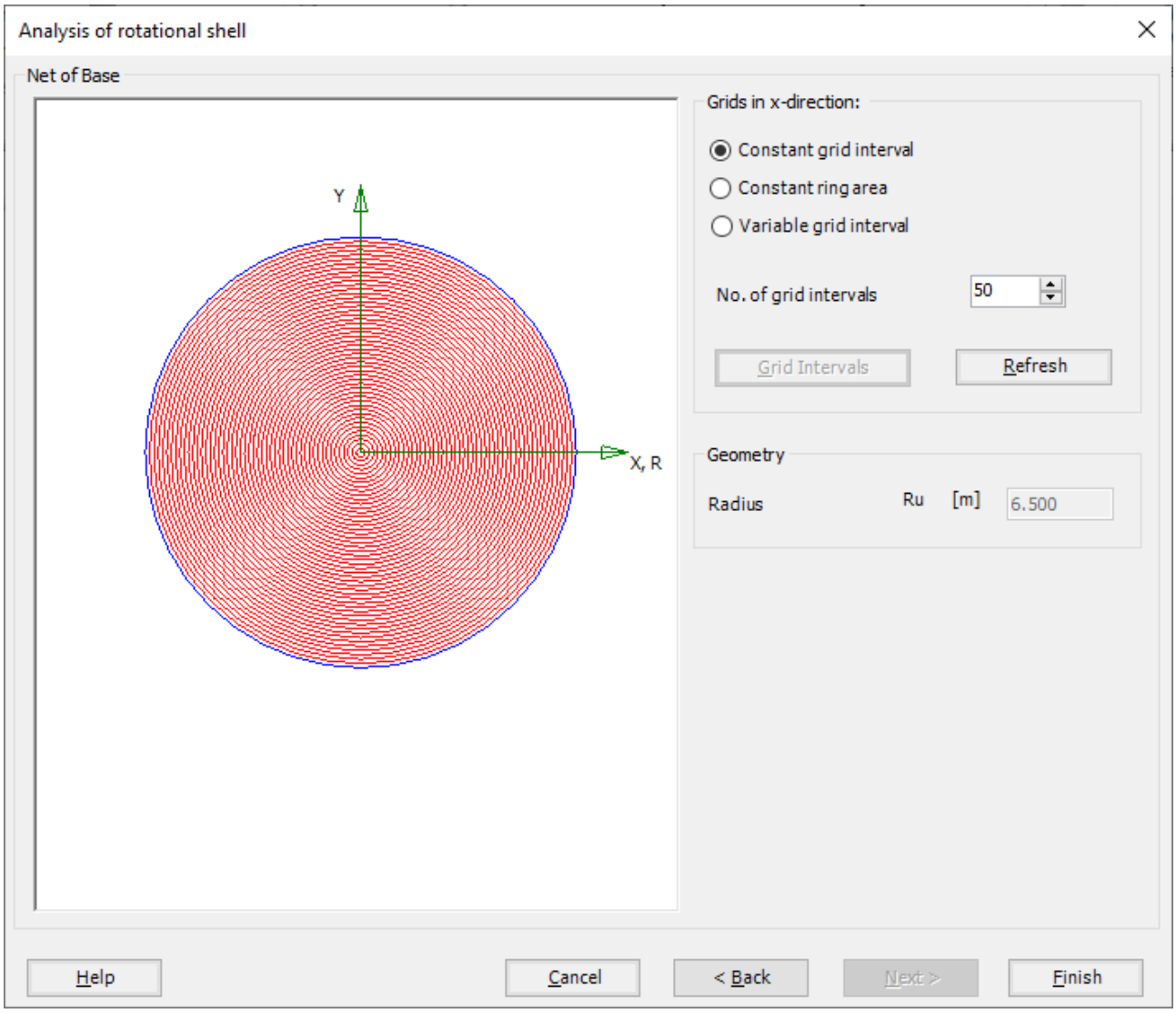

Figure 6.10 "Net of Base" Form

Click "Finish" button, the FE-Net of the tank wall and a sector from the base appear in Figure 6.11

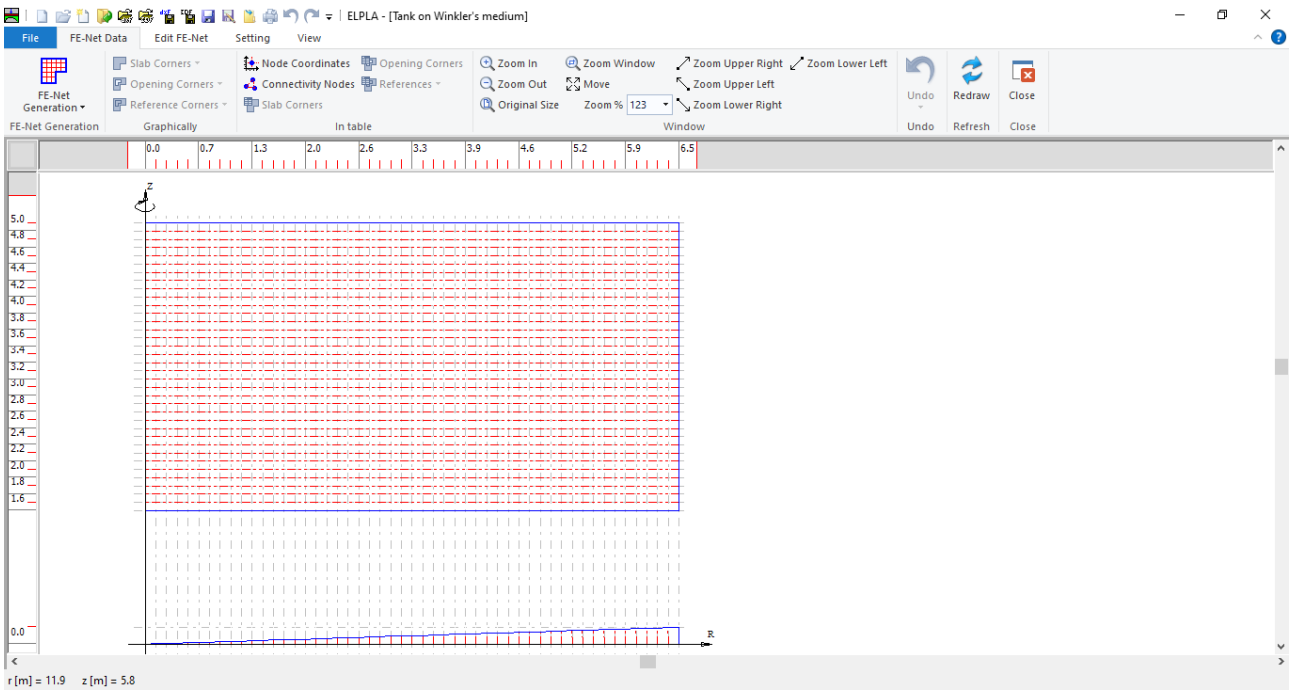

Figure 6.11 Generated FE-Net

After finishing the generation of the FE-Net, do the following two steps:

- Choose "Save" command from "File" menu in Figure 6.11 to save the data of the FE-Net
- Choose "Close" command from "File" menu in Figure 6.11 to close the "FE-Net" window and return to *ELPLA* main window

4.4 Shell properties

To define the tank properties, choose "Shell Properties" command from “Data” Tab. The following window in Figure 6.12 appears with default shell properties. The data of shell properties for the current example, which are required to be defined, are element groups, unit weight of the tank, and filled material properties.

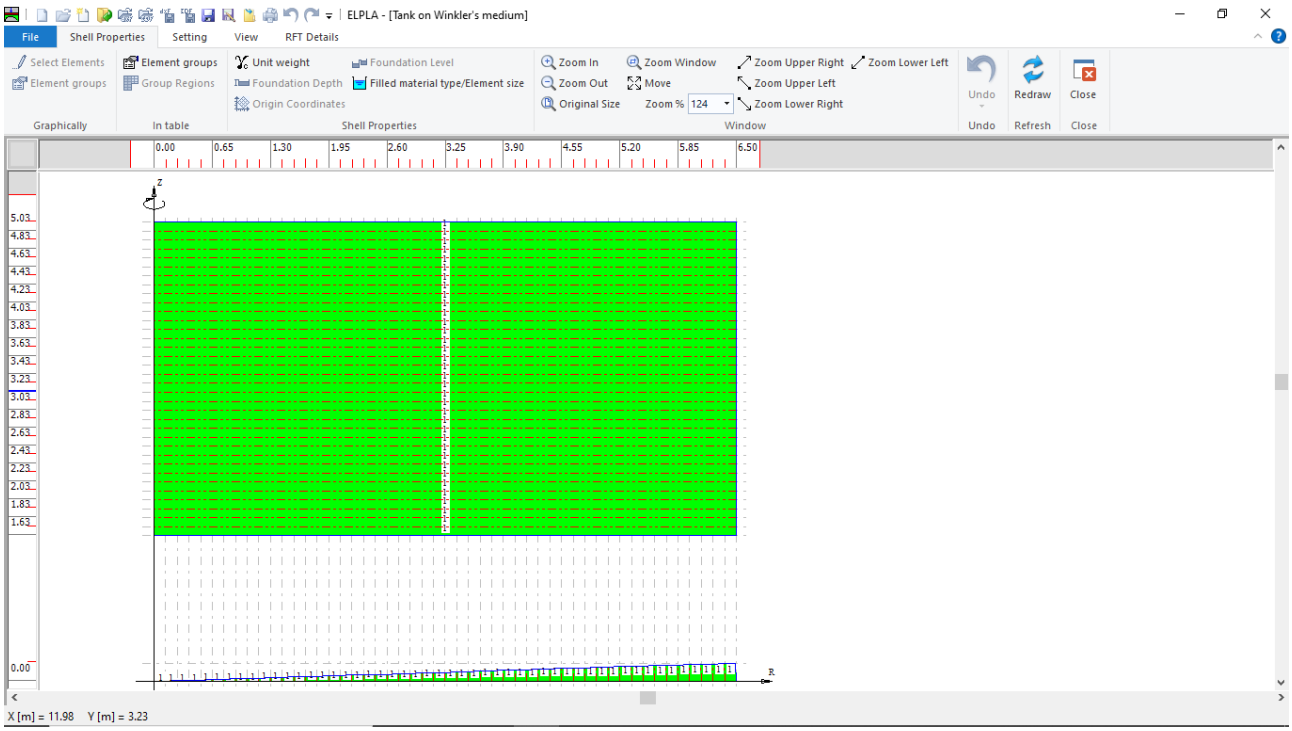

Figure 6.12 "Shell Properties" Window

Choose "Element groups" command from "In table" menu. The following list box in Figure 6.13 appears. In this list box, enter E-Modulus, *Poisson’s* ratio and slab thickness. Then click "OK" button.

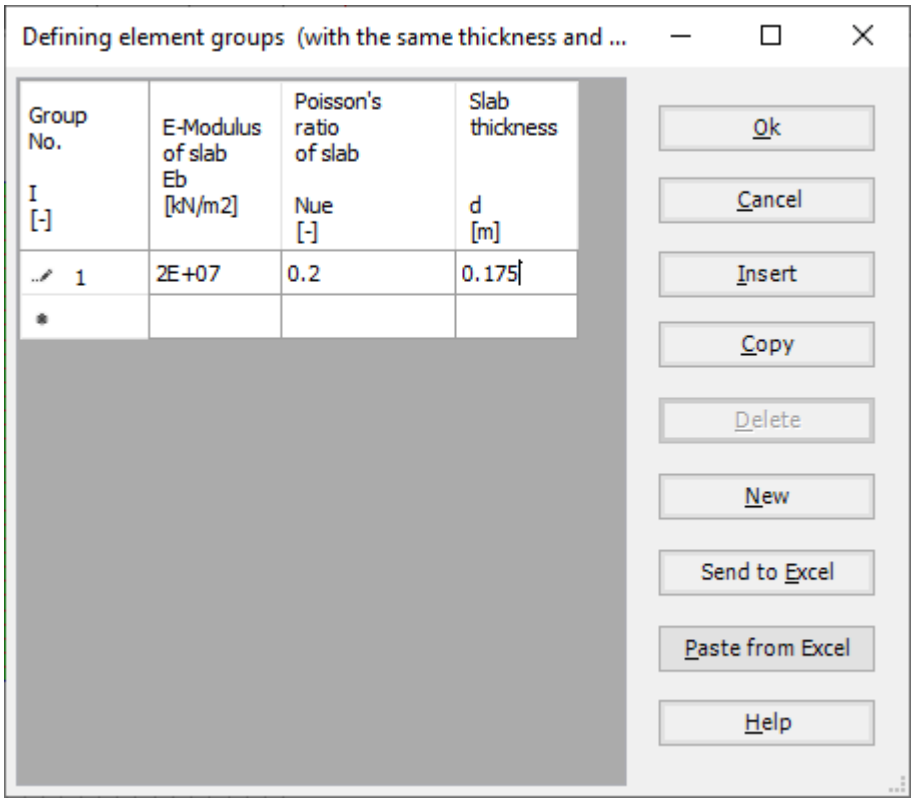

Figure 6.13 "Defining element groups" list box

To enter the unit weight of the tank, choose "Unit weight" command from "Shell Properties" menu in Figure 6.12. The following dialog box in Figure 6.14 with a default unit weight of 25 [kN/m^3] appears, click "OK" button.

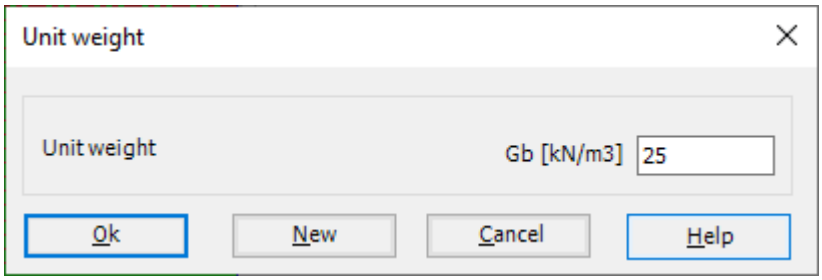

Figure 6.14 "Unit weight" dialog box

To define the liquid properties of the shell, choose "Filled material type/Element size" command from "Shell Properties" menu in Figure 6.12. The following form in Figure 6.15 appears.

To define the liquid properties of the tank:

- Select the "Liquid container" option
- Type 3.5 in the "Height of the liquid" edit box
- Type 10 in the "Unit weight of the liquid" edit box

To define the element size of the tank:

- Check the "Constant element sizes in z-direction" check box
- Type 1 in the "Element size in each shell segment" edit box. The element size is chosen to be 1 [m] larger than the segment size in order to ignore further subdivision of the segments into smaller elements. In some cases, it is necessary to divide the segment into smaller elements in order to make the analysis more precise. Nevertheless, the final results of the internal forces appear only at nodes of segments
- Click "OK" button

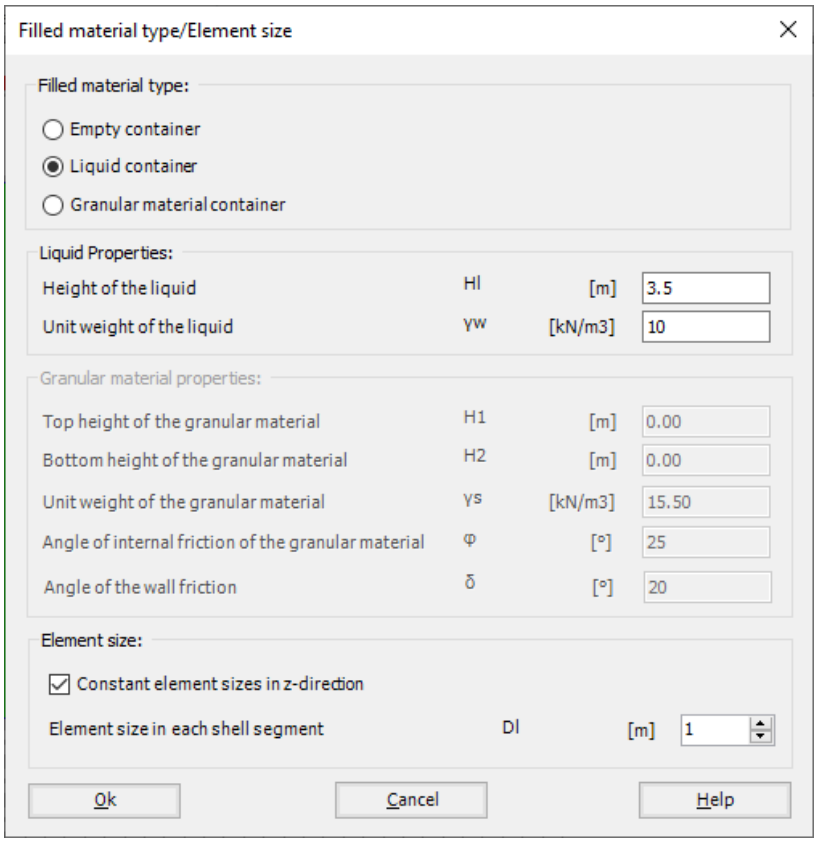

Figure 6.15 "Liquid properties/Element size" Form

After entering the shell properties, do the following two steps:

- Choose "Save" command from "File" menu in Figure 6.12 to save the shell properties
- Choose "Close" command from "File" menu in Figure 6.12 to close the "Shell properties" window and return to *ELPLA* main window

4.5 Soil Properties

To define the soil properties, choose "Soil Properties" command from “Data” Tab. The following "Soil Properties" form in Figure 6.16 appears, enter the modulus of subgrade reaction of the soil and the ground water depth under the ground surface. Other data for this example is not required.

Soil data

Modulus of subgrade reaction	k_s	= 100 000	[kN/ m^3]
Ground water depth under the surface	*Gw*	= 1	[m]

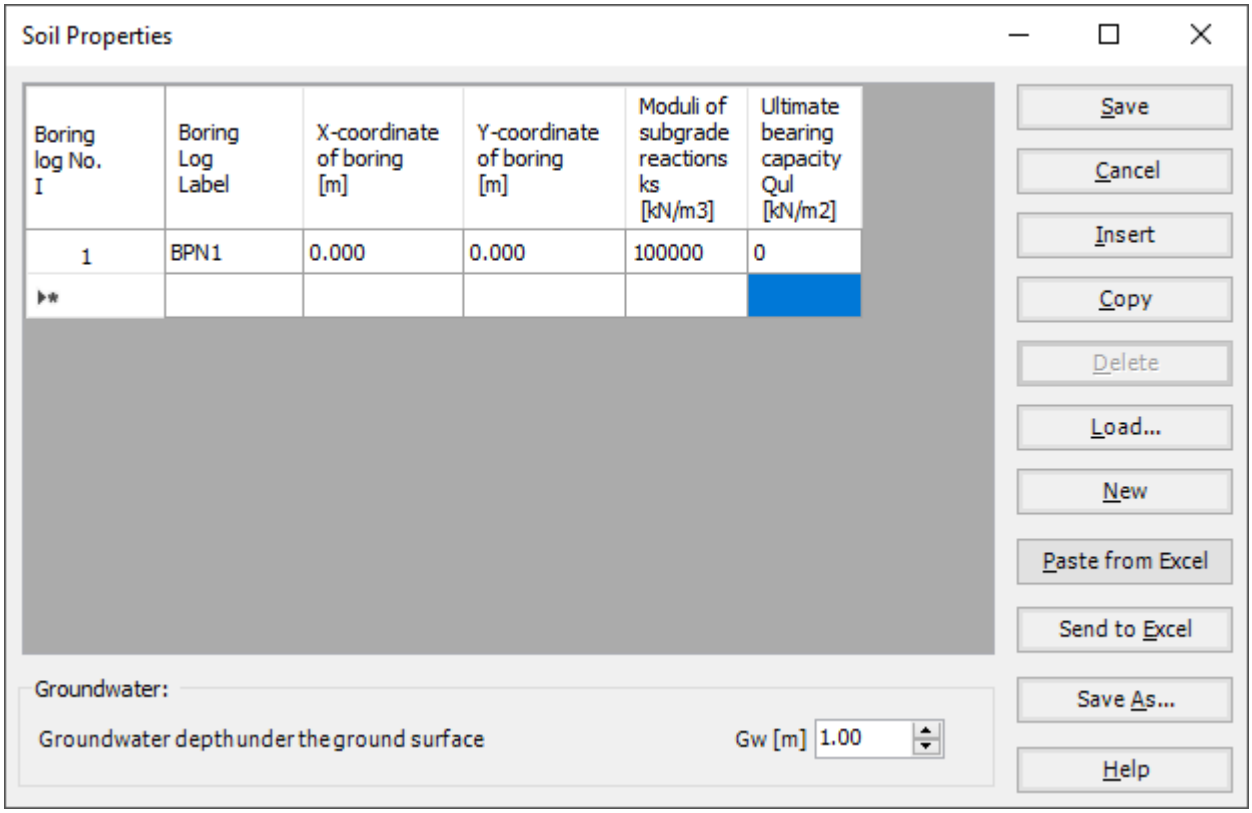

Figure 6.16 "Soil Properties" Form

4.6 Loads

To define the loads, choose "Loads" command from “Data” Tab. The following window in Figure 6.17 appears. In *ELPLA*, entering loads may be carried out either numerically (in a table) or graphically using the commands of "Loads" tab in Figure 6.17. In this example, there is not applied load, as the vertical load has been already defined by the unit weight of the tank, while the hydrostatic pressure on the tank wall is defined by the unit weight of water.

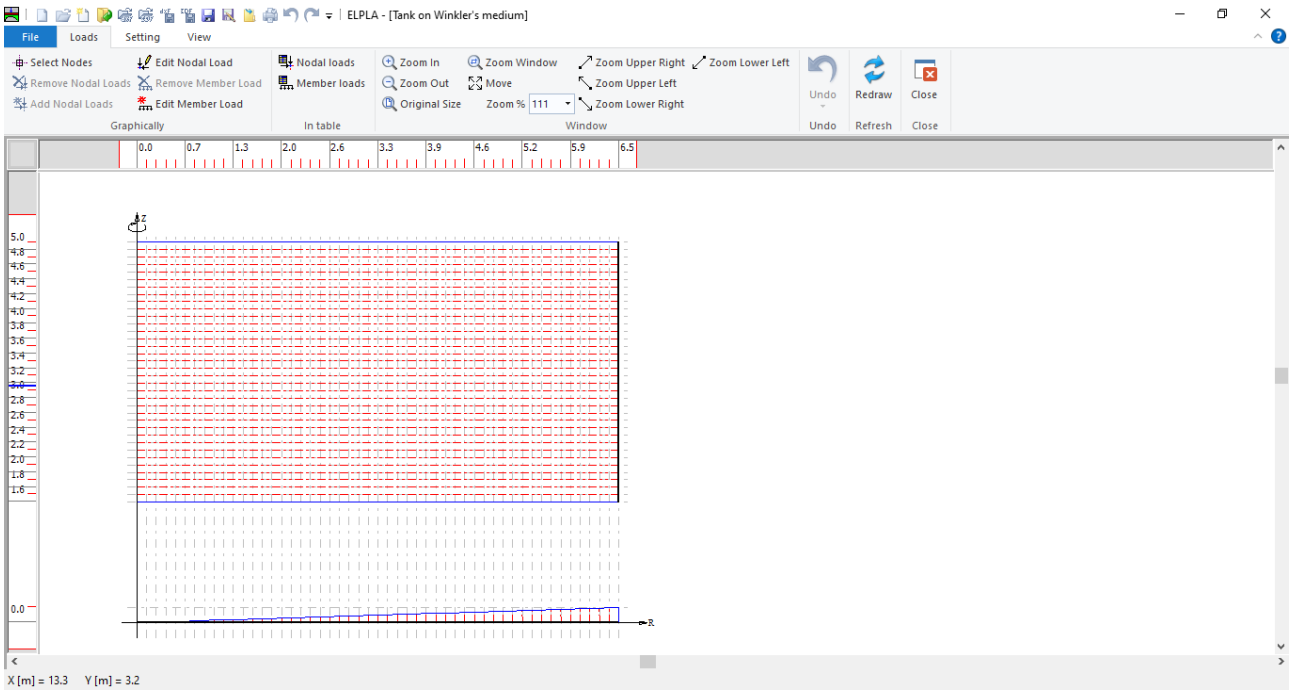

Figure 6.17 "Loads" Window

After finishing the definition of load data, do the following two steps:

- Choose "Save" command from "File" menu in Figure 6.17 to save the load data
- Choose "Close" command from "File" menu in Figure 6.17 to close the "Loads" window and return to *ELPLA* main window

Creating the project of the tank is now complete. It is time to analyze this project. In the next section, you will learn how to use *ELPLA* for analyzing projects.

5 Carrying out the calculations

To analyze the problem, switch to "Solver" Tab, Figure 6.18.

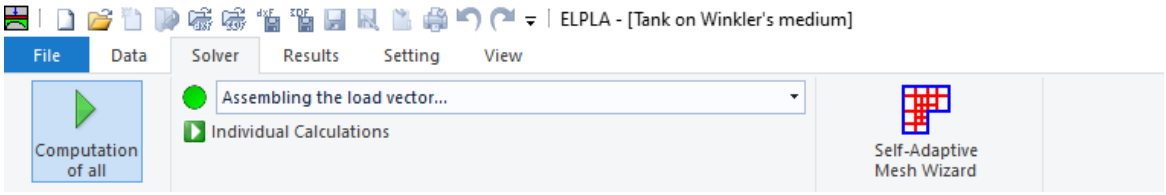

Figure 6.18 "Solver" Tab

ELPLA will active the "Individual Calculations" list, which contains commands of all calculations. Commands of calculation depend on the used calculation method in the analysis. For this project, the items that are required to be calculated are:

- Assembling the load vector
- Determining the modulus of subgrade reaction
- Assembling the slab stiffness matrix
- Solving the system of linear equations (band matrix)
- Determining deformation, internal forces, contact pressures

These calculation items can be carried out individually or in one time

To carry out all computations in one time

- Choose "Computation of all" command from "Solver" Tab Window.

The progress of all computations according to the defined method will be carried out automatically with displaying Information through menus and messages.

Analysis progress

Analysis progress menu in Figure 6.19 appears in which various phases of calculation are progressively reported as the program analyzes the problem. In addition, a status bar down of the "Solver" Tab window displays Information about the progress of calculation.

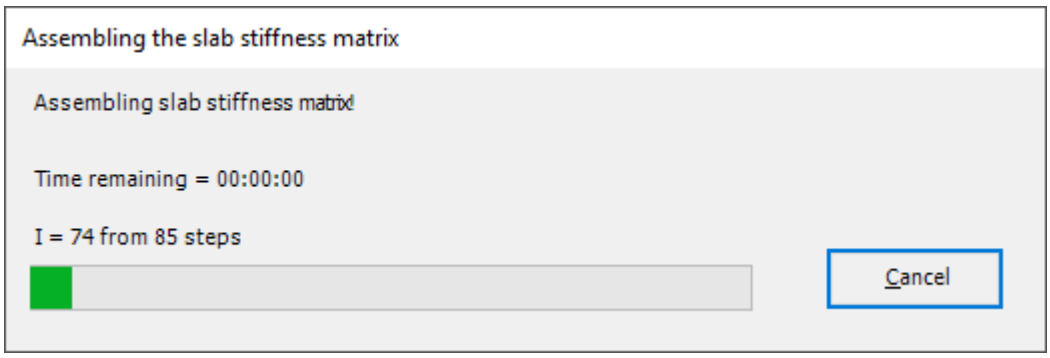

Figure 6.19 Analysis progress menu

Check of the solution

Once the analysis is carried out, a check menu of the solution appears, Figure 6.20. This menu compares between the values of actions and reactions. Through this comparative examination, the user can assess the calculation accuracy.

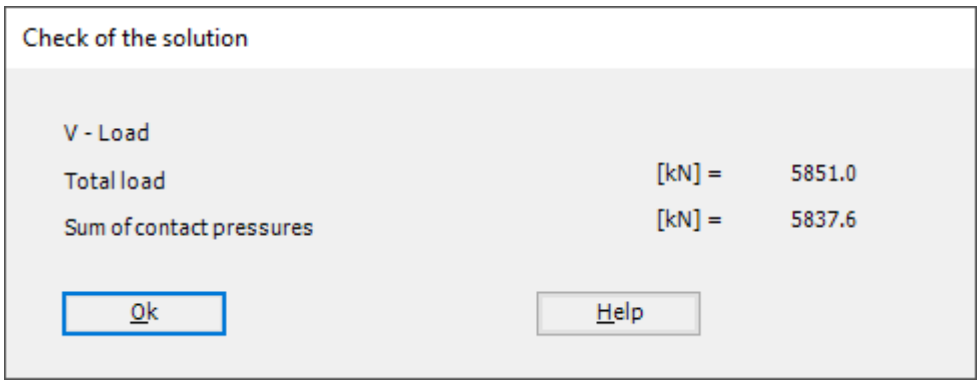

Figure 6.20 Menu "Check of the solution"

Click "OK" button to finish analyzing the problem.

6 Viewing data and results

ELPLA can display and print a wide variety of results in graphics, diagrams or tables through the "Results" Tab.

To view the data and results of a problem that has already been defined and analyzed graphically, switch to "Results" Tab (Figure 6.21).

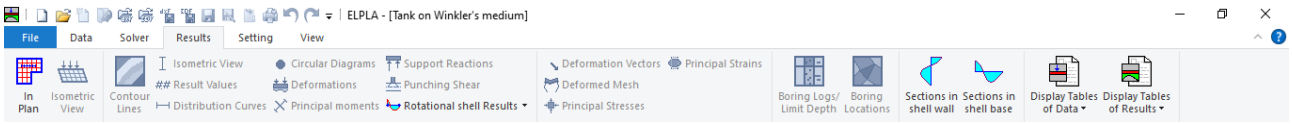

Figure 6.21 "Results" Tab

The "Results" Tab contains the commands of drawing. These commands depend on the used calculation method in the analysis. For the current example, the commands for presenting the data and results are:

- Data in the plan
- Rotational shell results
- Sections in shell wall
- Sections in shell base
- Display tables of data
- Display tables of results

To view the radial forces in the shell wall

- Choose "Sections in shell wall" command from "Section" menu. The following option box in Figure 6.22 appears
- In the "Sections in shell wall" option box, select "Radial forces *Nr*" as an example for the results to be displayed
- Click "OK" button

The Results are now displayed as shown in Figure 6.23.

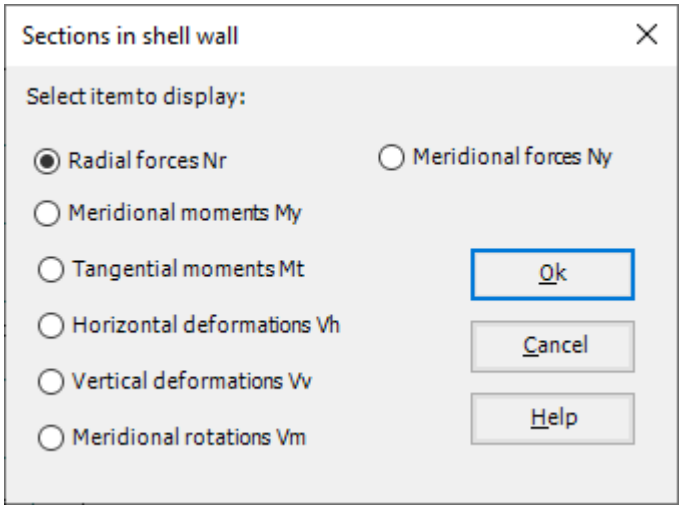

Figure 6.22 "Sections in shell wall" option box

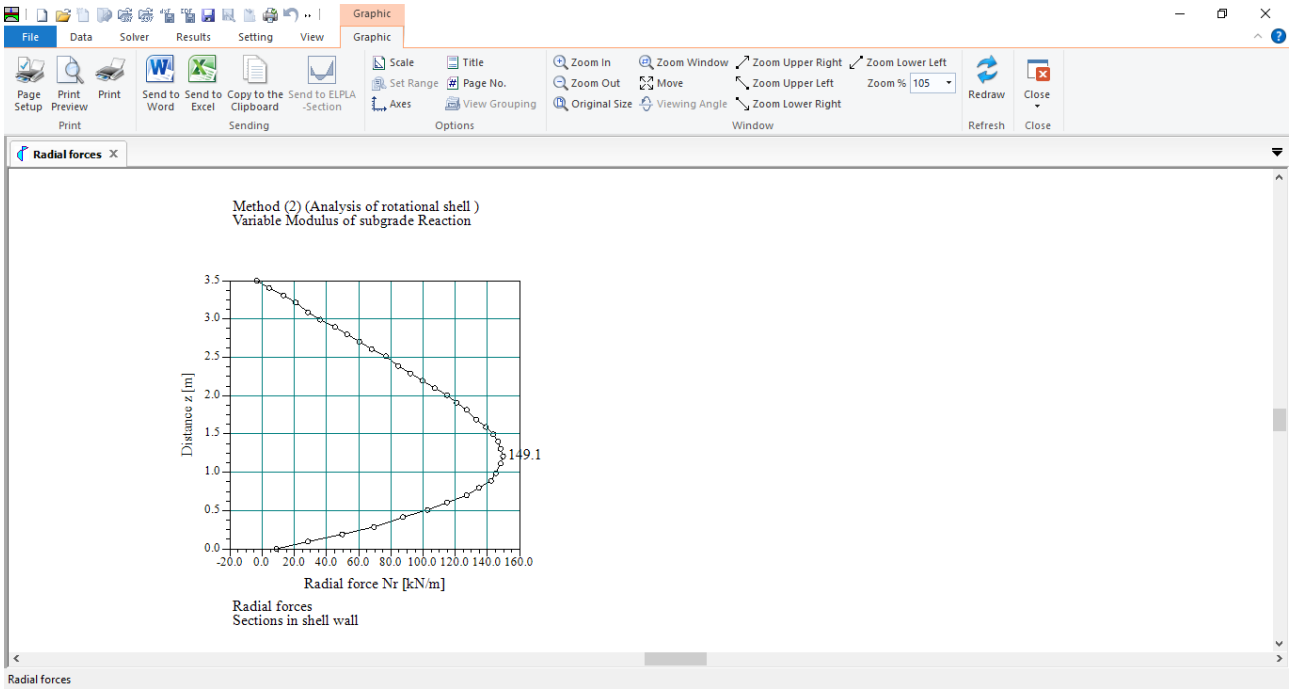

Figure 6.23 Radial forces in shell wall

To view the meridional moments on the shell wall

- From "Rotational shell results" command in the "Results" menu, choose "In Plan" command, the following option box in Figure 6.24 appears
- In the "Distribution of Internal Forces" option box, select "Meridional moments *My*" as an example for the results to be displayed
- Click "OK" button

The Results are now displayed as shown in Figure 6.23.

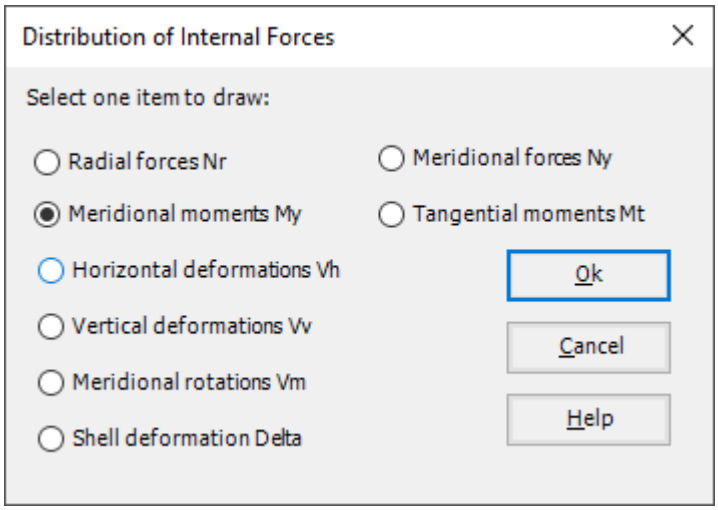

Figure 6.24 "Distribution of Internal Forces" option box

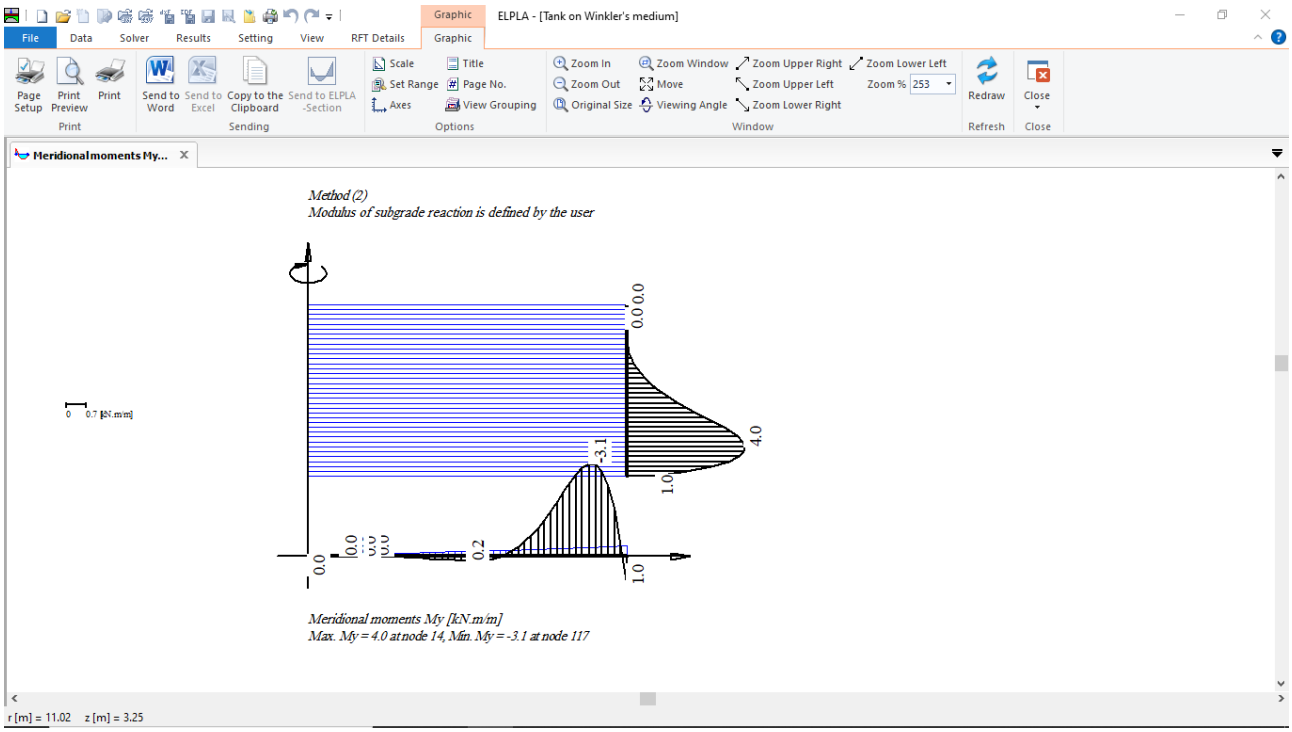

Figure 6.25 Meridional moments on the shell wall